

1. Repetition: connected components and other definitions
2. Theorem: # connected components $\geq |V| - |E|$
3. Definition of a tree: a connected graph with no cycles (as subgraphs)
4. Theorem: A graph G is a tree if and only if
 - (a) it is connected and deleting any edge results in a disconnected graph
 - (b) it is connected and $|E| = |V| - 1$
 - (c) there is exactly one path between each pair of vertices
5. Lemma ([1]:Theorem 8.2.1) Every tree with at least two nodes has at least two nodes of degree 1.
6. k -colorability
7. Theorem: A graph is 2-colorable if and only if it contains no odd cycle.

References

The books are listed on the wiki-page.

[1]: Sections 8.1, Theorem 8.2.1, Theorem 13.2.1

[2] Chapter 6

[3]: Sections 3.2.5, 3.5.2

[4]: Sections 3.1, 3.2.1-3.2.3,

Keywords (that have not been aforementioned)

- *incident*: u incident with an edge $\{u, v\}$.
- *external vertex* (of a tree) is a vertex of degree 1
- *internal vertex* (of a tree) is a vertex that is not external
- *isolated vertex* is a vertex of degree 0